

# Stability analysis of a multi-camera photogrammetric system used for structural health monitoring

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# Structural health monitoring

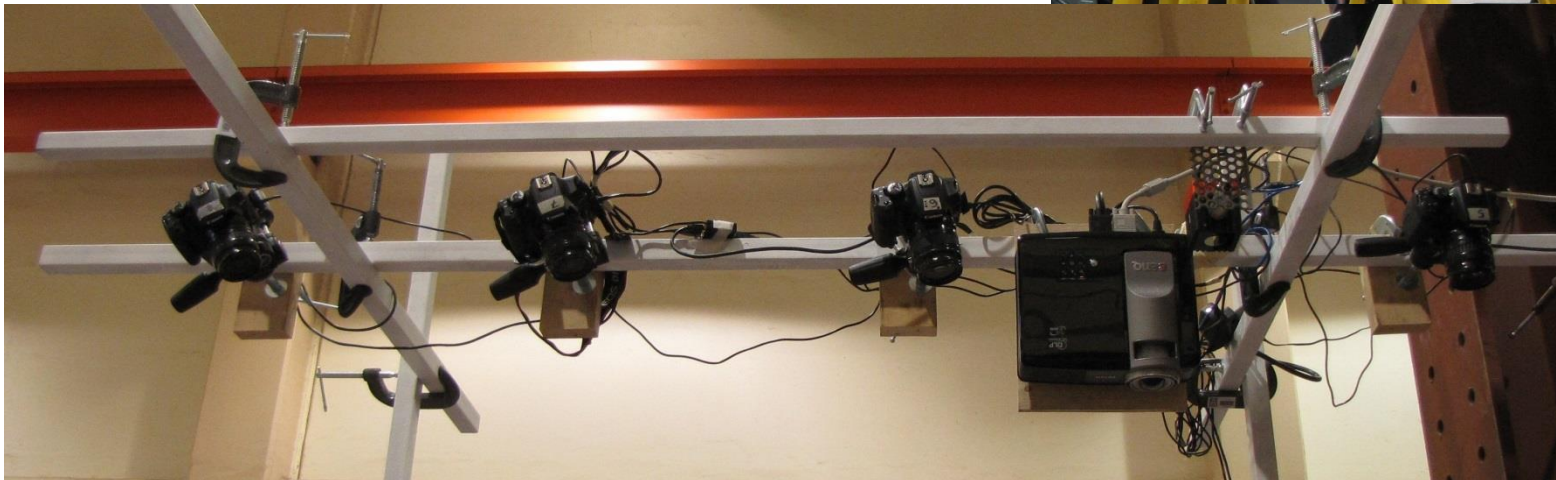
## Fine-scale level:

- Measurement of deflections and cracks in structural components
- Provision of feedback for structural design improvements



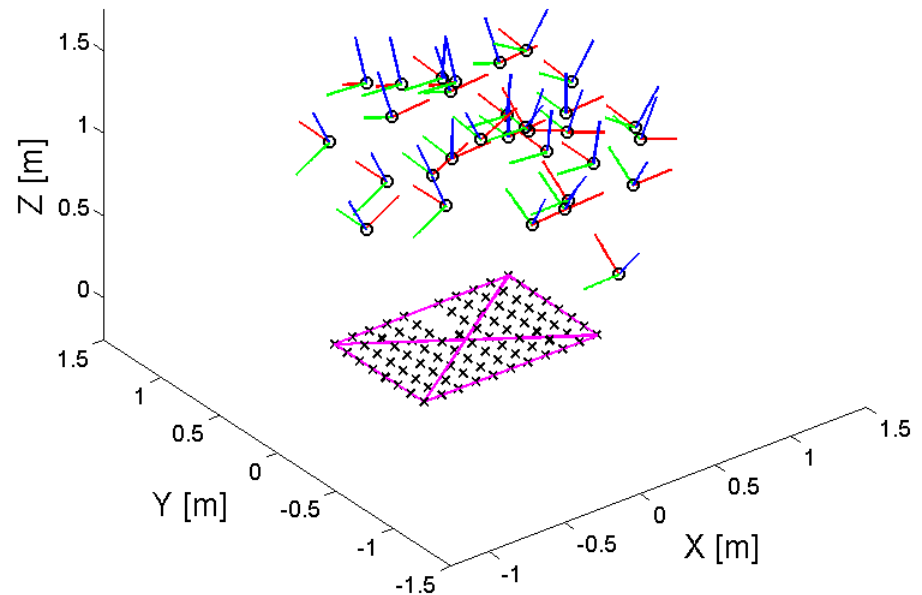
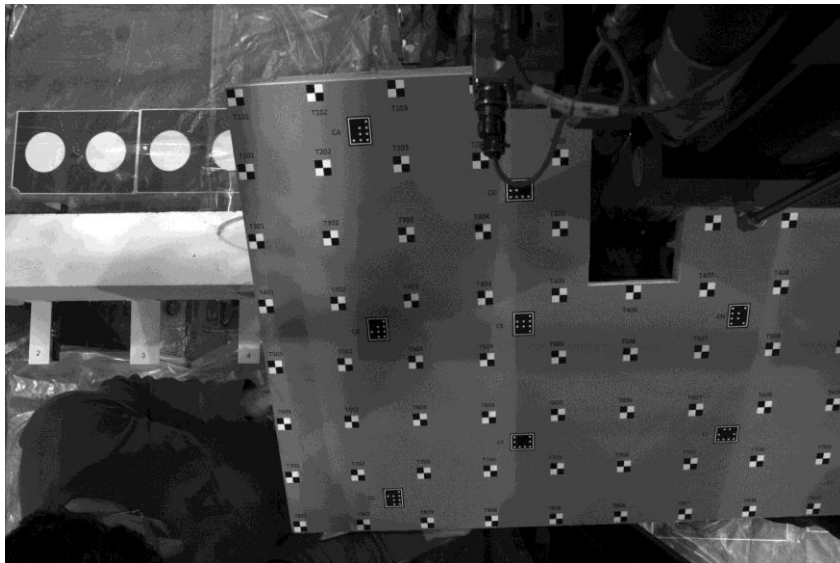
# Proposed photogrammetric systems

- Standing/upright system for crack observations
- Suspended/overhanging system for deflection measurements



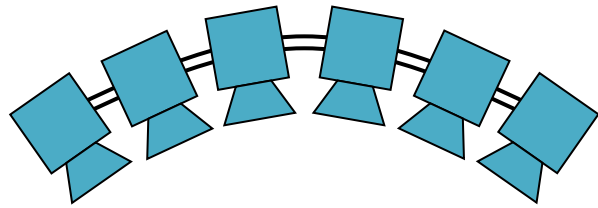
# In-situ multi-system calibration

- Series of rotations and translations of a portable 2D test field
- Simultaneous estimation of interior orientation (IOPs) and camera mounting (CMPs) parameters

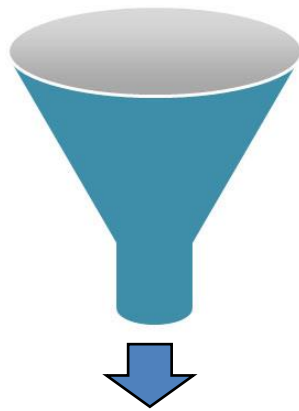
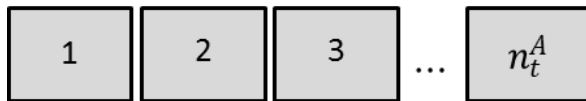


# System stability analysis

IOPs and CMPs at  $t_1$

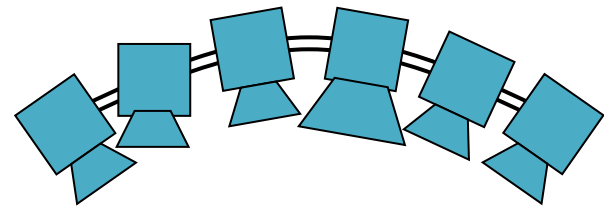


Block A

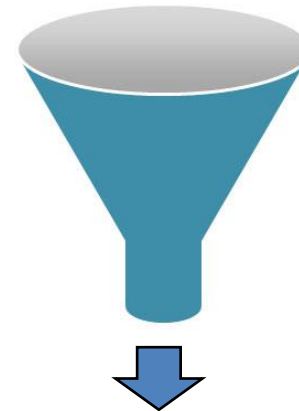
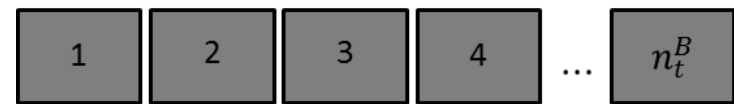


XYZ

IOPs and CMPs at  $t_2$



Block B



XYZ

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# System stability methodologies

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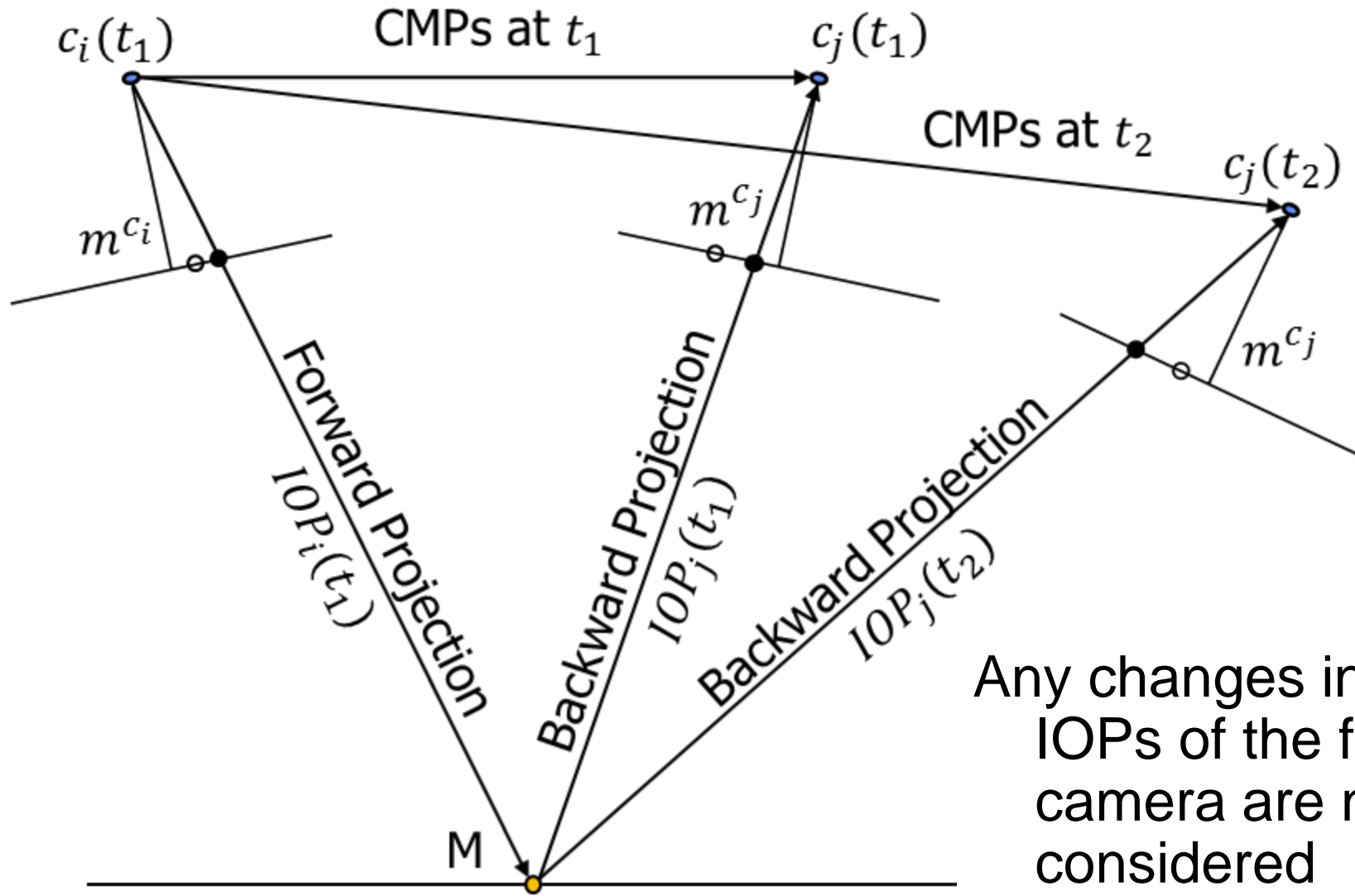
## Concept:

- Numerical tool for checking the impact of different sets of calibration parameters

## Methods:

- Method 1: combination of forward and backward projections
- Method 2: object space parallax in image space units
- Method 3: variation in normalized image coordinates

# Method 1



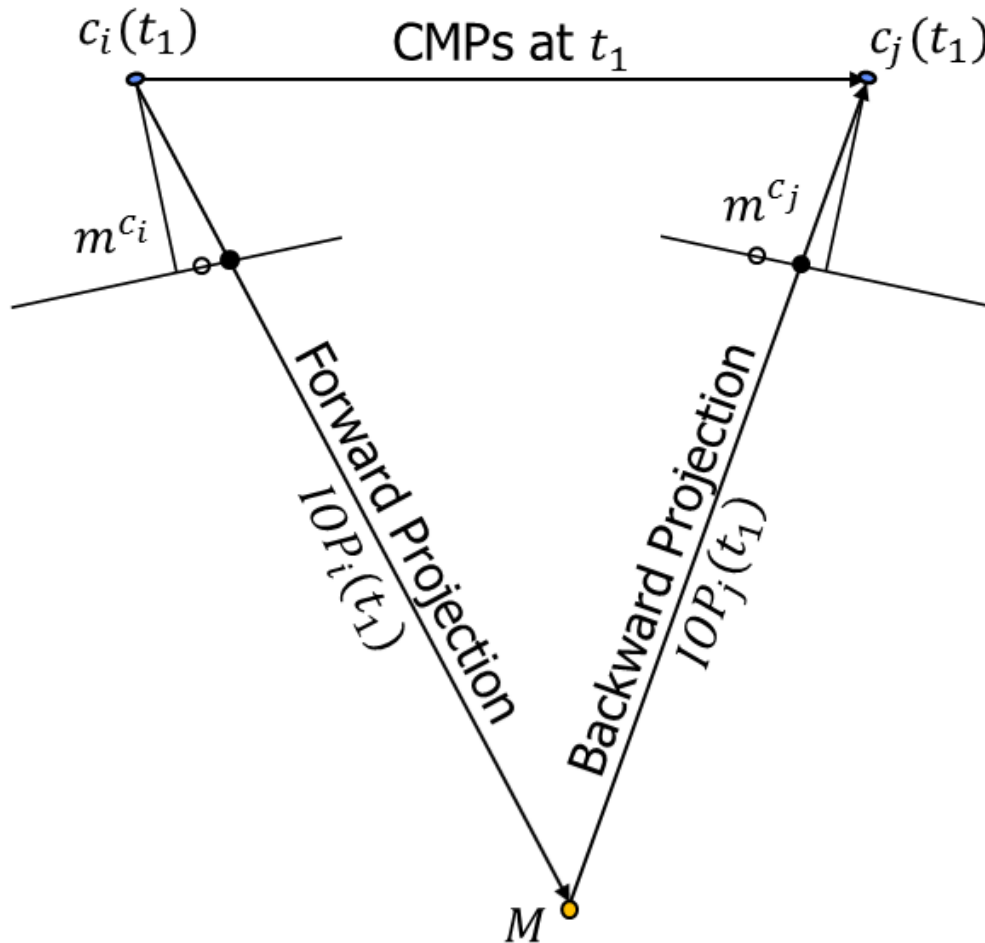
Any changes in the IOPs of the first camera are not considered



# Method 2 (1/2)

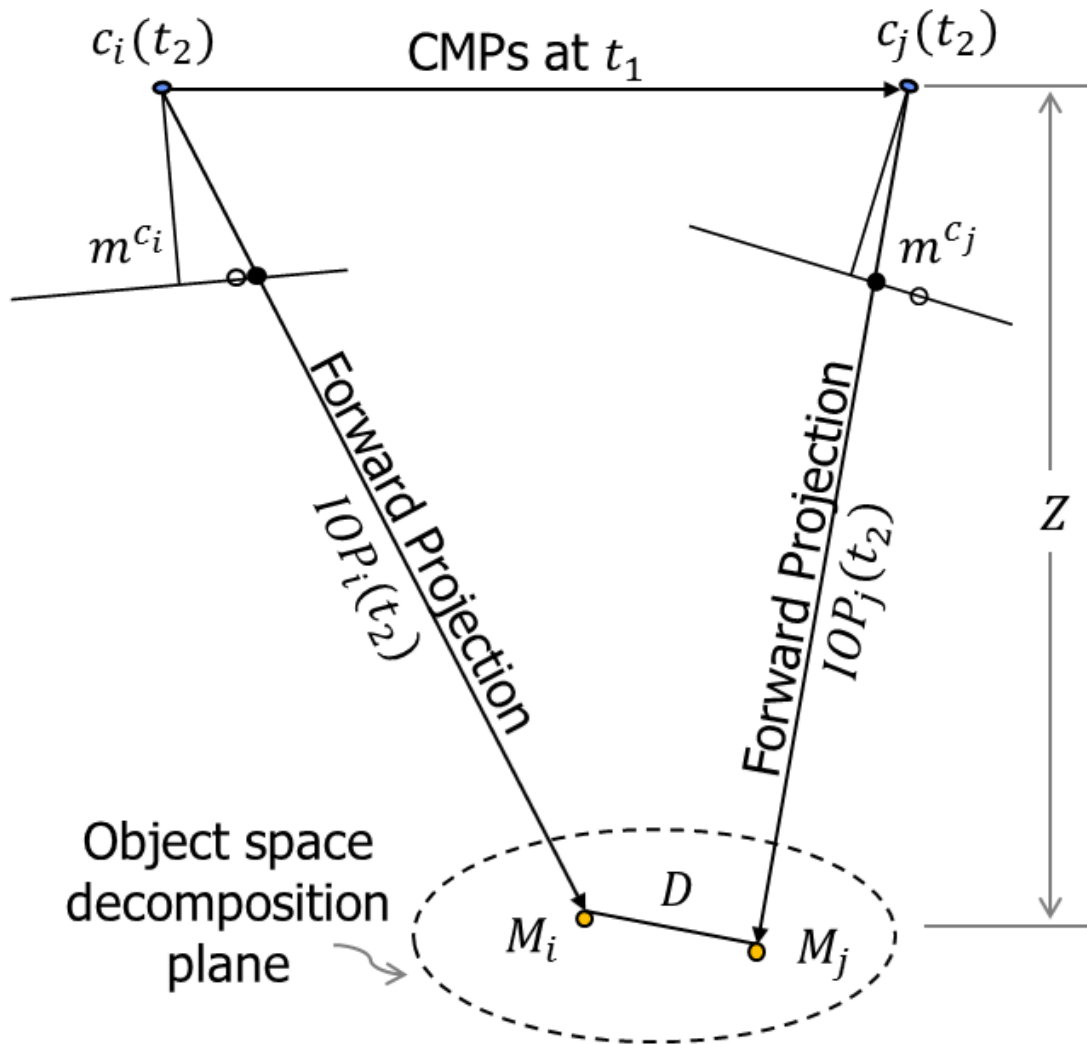
Obj

ts



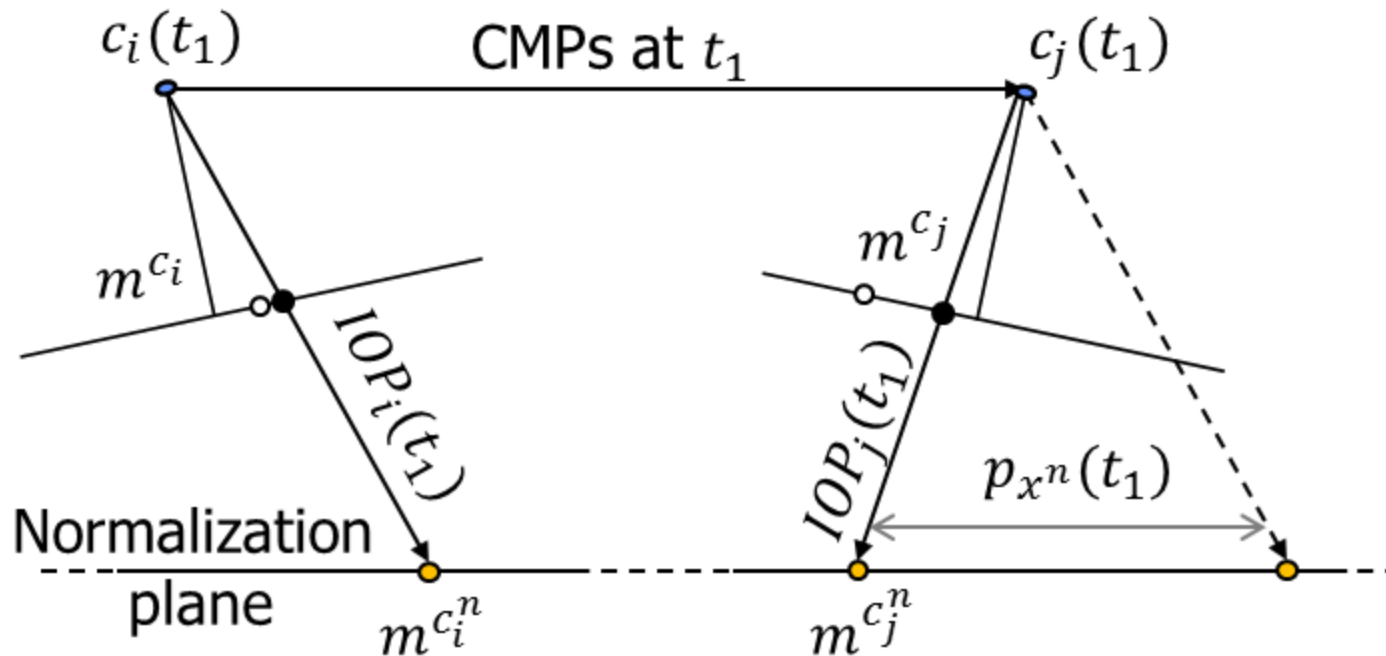


# Method 2 (2/2)



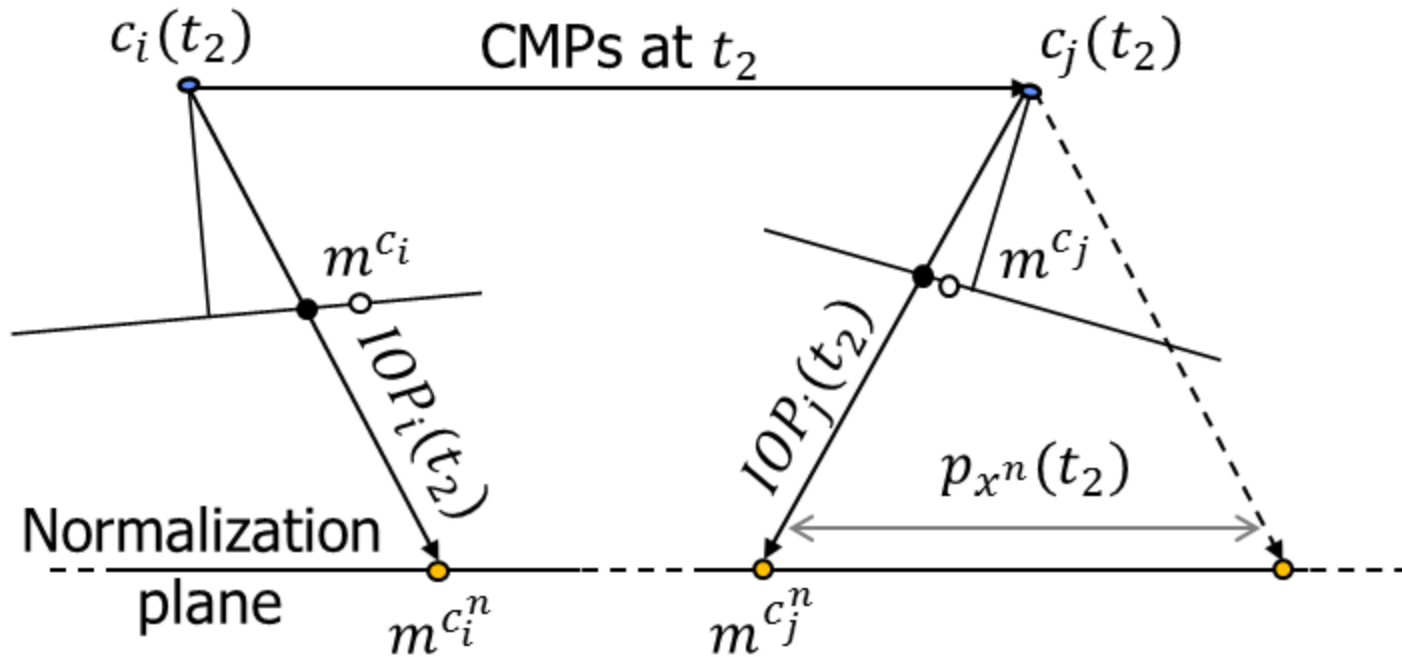
# Method 3 (1/2)

## Variation in the normalized image coordinates



# Method 3 (2/2)

## Variation in the normalized image coordinates



Any changes in the magnitude/extent of the baseline would not be picked up

# Conducted tests

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## Simulation of changes in the IOPs and CMPs

- Method 1 vs. Method 2 comparison
- Method 3 vs. Method 2 comparison
- Decide which method works best in the most general case

## Real world tests

- System stability analysis for a multi-day experiment
- Same-day system stability analysis
- Come up with recommendations on the frequency of calibration and/or locating any (source of) instability

# Simulation of changes in IOPs & CMPs

- Biases applied one by one to each odd-numbered camera in a system
- Magnitude of biases chosen to cause noticeable instability

Parameters	Biases	Units
$x_p, y_p, c$	+50 or +100	[ $\mu\text{m}$ ]
$k_1, k_2$	$+5 \times 10^{-5}$ or $+5 \times 10^{-7}$	[ $\text{mm}^{-2}$ ] or [ $\text{mm}^{-4}$ ]
$p_1, p_2$	$+1 \times 10^{-5}$	[ $\text{mm}^{-1}$ ]
$b_x, b_y, b_z$	+5	[mm]
$b_\omega, b_\varphi, b_\kappa$	+0.1	[ $^\circ$ ]

# Changes in the IOPs (1/2)

Parameters / cam pairs	Method 1	Method 2	Method 3
	Total RMSE [px] for Cams 4 & 5		
None	0.00	0.00	0.00
$\Delta x_p$	8.76	8.96	8.98
$\Delta y_p$	8.76	8.95	8.91
$\Delta c$	5.25	5.43	5.47
$\Delta k_1$	4.85	4.95	5.03
$\Delta k_2$	5.15	5.17	5.26
$\Delta p_1$	0.27	0.28	0.29
$\Delta p_2$	0.16	0.17	0.17

# Changes in the IOPs (2/2)

Parameters / cam pairs	Method 1	Method 2	Method 3
	Total RMSE [px] for Cams 3 & 4		
None	0.00	0.00	0.00
$\Delta x_p$	0.00	8.83	8.90
$\Delta y_p$	0.00	8.82	8.84
$\Delta c$	0.00	6.18	4.46
$\Delta k_1$	0.00	2.84	2.91
$\Delta k_2$	0.00	2.17	2.23
$\Delta p_1$	0.00	0.18	0.19
$\Delta p_2$	0.00	0.13	0.13

Method 1 does not perform adequately in the scenario when the IOPs of the first camera are changed

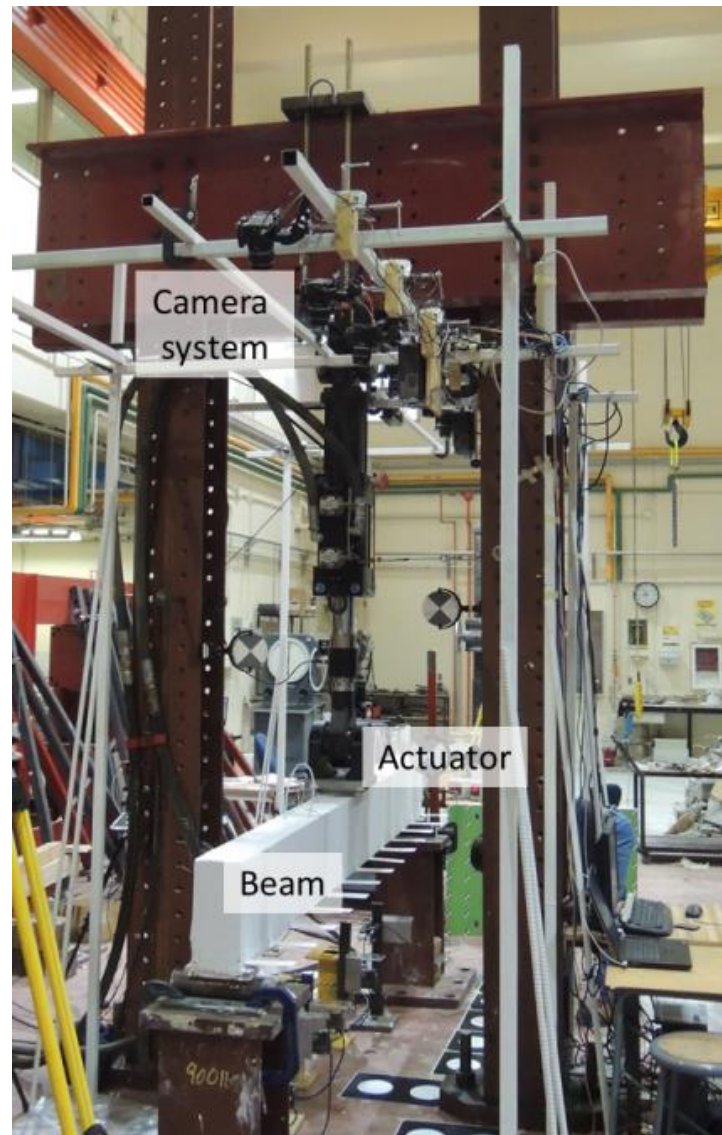
# Changes in the CMPs

Parameters / cam pairs	Method 1	Method 2	Method 3
	Total RMSE [px] for Cams 3 & 4		
None	0.00	0.00	0.00
$\Delta b_X$	10.57	11.05	0.15
$\Delta b_Y$	10.62	10.89	10.91
$\Delta b_Z$	3.15	3.40	4.48
$\Delta b_\omega$	6.86	7.04	7.05
$\Delta b_\varphi$	6.70	7.01	7.27
$\Delta b_\kappa$	1.72	1.76	1.77

Method 3 does not perform adequately in the scenario when there are changes in the extent of the baseline



# Example photogrammetric system (1/2)



Suspended /  
overhanging  
system for  
deflection  
measurements

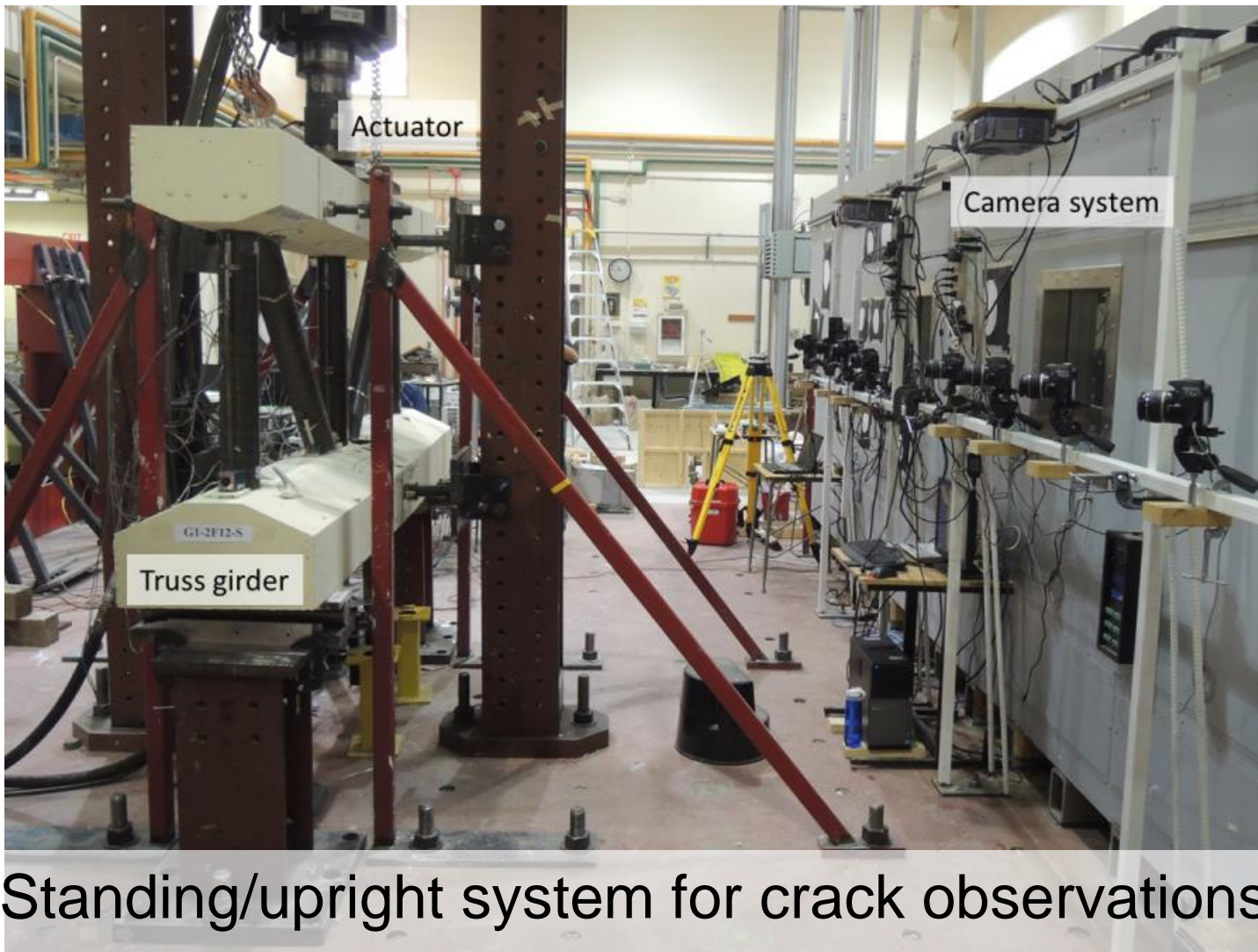
# Multi-day system stability test

Cam pairs / RMSEs	Total RMSE [px]	
	Day 1 vs. Day 2	Day 2 vs. Day 3
Cams 1 & 2	0.64	0.92
Cams 2 & 3	1.02	1.02
Cams 3 & 4	0.44	0.56
Cams 4 & 5	1.05	0.48
Cams 5 & 6	1.75	0.60
Cams 6 & 7	1.09	0.71
Cams 7 & 8	1.10	2.41



Increase the calibration frequency from once to twice daily (i.e., before start and after end of each daily experiment)

# Example photogrammetric system (2/2)



# Same day system stability test

Cam pairs / RMSEs	Total RMSE [px]	
	Pre vs. Mid	Mid vs. Post
Cams 1 & 2	0.96	0.28
Cams 2 & 3	0.39	0.66
Cams 3 & 4	0.21	0.41
Cams 4 & 5	0.79	0.33
Cams 5 & 6	0.53	0.24
Cams 6 & 7	0.72	0.68
Cams 7 & 8	1.55	1.02



Potential source of instability in the vicinity of Cam 8

# Conclusions

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Three methods for performing system stability analysis were presented:

- All based on synthetic grids in image space, and pairwise relationship between neighbouring cameras
- Method 2 yields the best measure of (in)stability in the most general case
- Results help with deciding on the required frequency of calibration
- Any system instability can be pin-pointed, and potentially mitigated

# Acknowledgements

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# Thank you!

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**DPRG**

Digital Photogrammetry  
Research Group



# Traditional instrumentation

## Deflection measurements

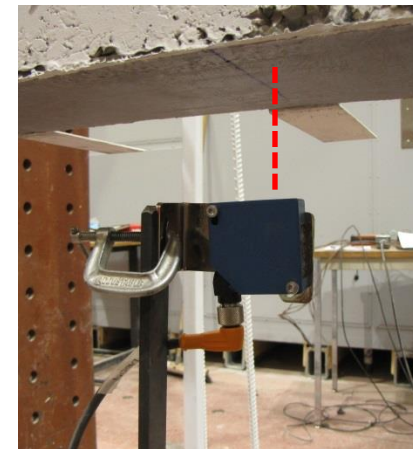
- Laser transducers, fibre optic sensors, wire strain gauges



[http://www.instron.com/fileuniverse/live/images/Accessories/2601-093\\_P.jpg](http://www.instron.com/fileuniverse/live/images/Accessories/2601-093_P.jpg)

## Crack observations

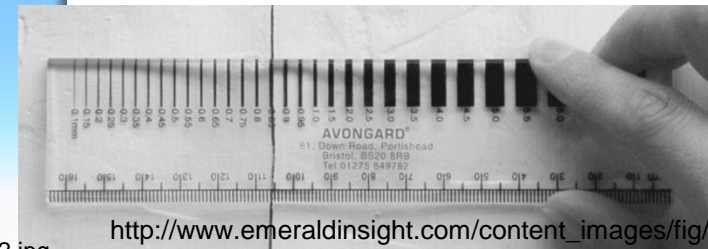
- Strain gauges, crack oculars, crack width templates



[http://upload.wikimedia.org/wikipedia/commons/b/b1/Hudson-Athens\\_Strain\\_Gauge.jpg](http://upload.wikimedia.org/wikipedia/commons/b/b1/Hudson-Athens_Strain_Gauge.jpg)



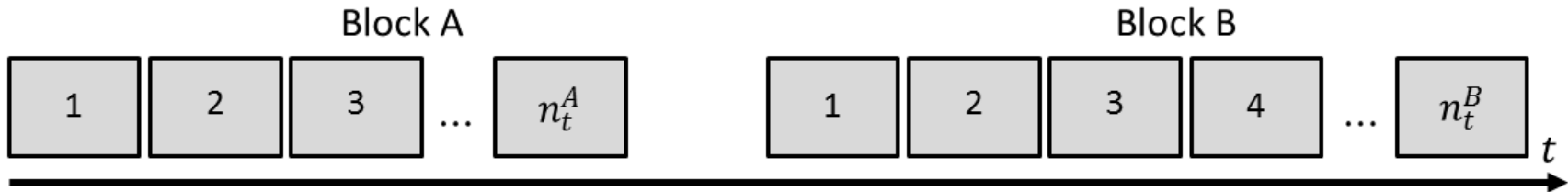
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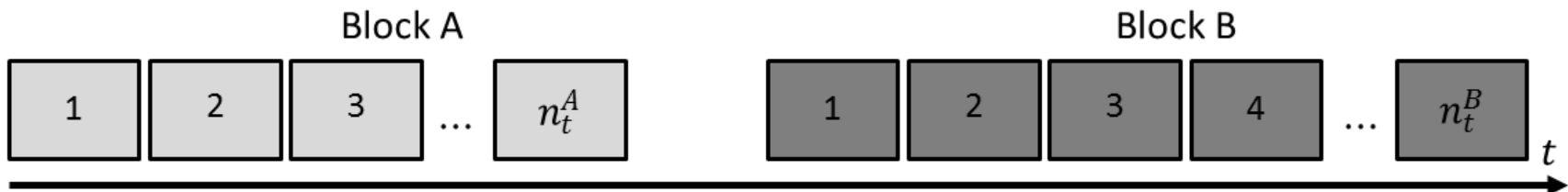
[http://www.emeraldinsight.com/content\\_images/fig/](http://www.emeraldinsight.com/content_images/fig/)

# Camera (in)stability scenarios

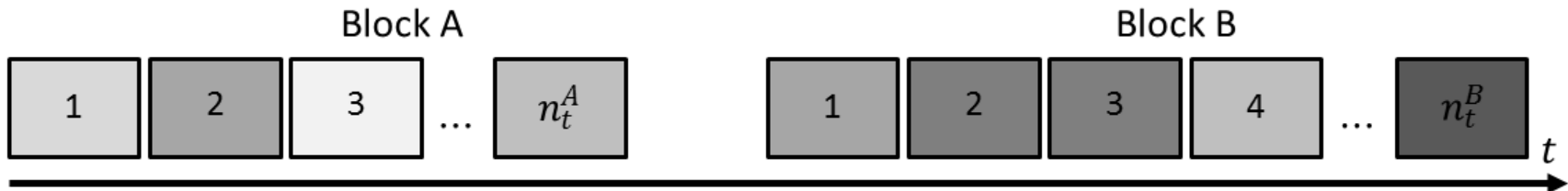
## a) No instability



## b) Instability between different blocks



## c) Instability within a block



# System stability analysis

Do the 3D reconstruction results differ depending on the set of system calibration parameters used?

