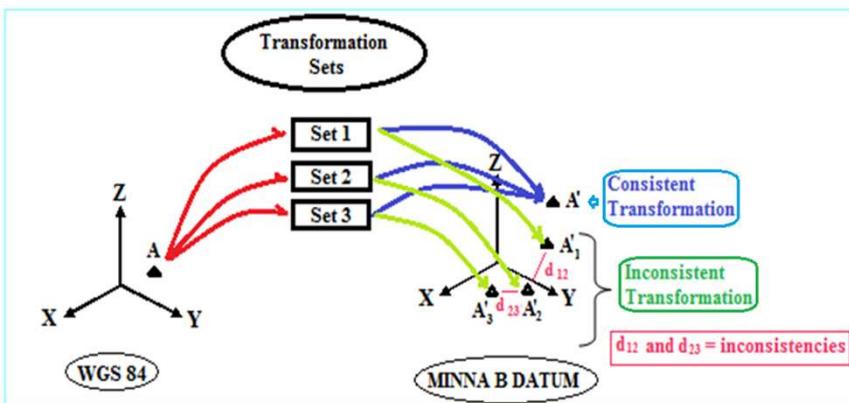


Removal of Inconsistencies Arising from Multiplicity of Transformation Parameters in Nigeria

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INTRODUCTION

CONSISTENT AND INCONSISTENT TRANSFORMATIONS



THE CHALLENGE OF MULTIPLICITY OF TRANSFORMATION PARAMETERS IN NIGERIA

- ▶ In the Nigerian Petroleum industry very many transformation sets are applied by different Companies for transforming WGS84 coordinates to Minna datum .
- ▶ Geodetic computations in Nigeria face challenges from this multiplicity of transformation parameters because transformations done for a given point with these different sets differ sometimes by as much as 45 meters.
- ▶ This is particularly a major challenge in the Nigerian Petroleum industry because wrongly transformed coordinates can lead to wrong location of an oil-well head, so that, instead of drilling oil, water may be drilled! Or at best, drilling may hit oil, but, at the wrong elevation!
- ▶ Another dimension to this challenge is the fact that some of these transformation sets (e.g. DMA parameters) are embedded in the configuration suites of GPS instruments which are used to determine Minna B datum coordinates during field observations. These usually differ from those determined from the transformation sets officially used by other companies.
- ▶ This situation exists because the Nigerian Government is still working on an official WGS84/Minna datum transformation set.

GEODETIC NETWORKS IN NIGERIA(1)

▶ 1. GPS Networks in Nigeria

- In 2009/2010 the Federal government of Nigeria established eleven (11) Continuously Operating Reference Stations (CORS) located at strategic positions in the country
- Many Oil Companies operating in the Niger Delta region of the country had established various GPS control networks to facilitate their oil exploration operations.
- All these GPS networks are reduced and computed on the World Geodetic System of 1984 (WGS84 – datum) which uses a geocentric ellipsoid with the following dimensions:
 - $a = 6378137.0 \text{ m}$
 - $f = 1/298.257223563$

GEODETIC NETWORKS IN NIGERIA(2)

► 2. The Nigerian (Minna B) Geodetic Network

- Nigeria is covered with first-order triangulation chains and traverse control networks.
- These networks were computed on a local geodetic datum called “Minna B” datum with its origin located at station L40 (the northern terminal of the Minna base of the Nigerian Primary triangulation network).
- The Minna B datum is based on the Clarke 1880 ellipsoid (Semi-major axis, $a = 6378249.145\text{m}$; Flattening, $f = 1/293.465$).
- The L40 origin has the following adopted geodetic coordinates (Uzodinma and Ezenwere, 1993):
 - Latitude $\phi = 09^\circ 38' 09'' \text{N}$
 - Longitude $\lambda = 06^\circ 30' 59'' \text{E}$
 - Height, $H = 279.6\text{m}$ above the geoid.

Interconversions between a Global and Local Datum

- The Molodensky-Badekas model is considered the best model for datum transformation between a global (e.g. WGS84) and local datum (e.g. the Minna B datum).
- The model in its matrix-vector form could be written as (Al Marzooqi, Y et al, 2005):

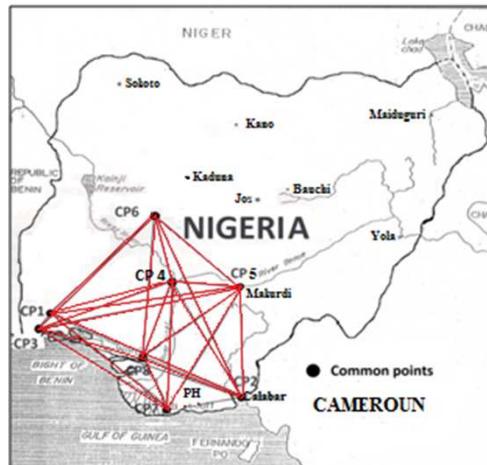
$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} \Delta X \\ \Delta Y \\ \Delta Z \end{bmatrix} + \begin{bmatrix} X_M \\ Y_M \\ Z_M \end{bmatrix} + \begin{bmatrix} 1 + \Delta L & R_Z & -R_Y \\ -R_Z & 1 + \Delta L & R_X \\ R_Y & -R_X & 1 + \Delta L \end{bmatrix} \begin{bmatrix} X' - X_M \\ Y' - Y_M \\ Z' - Z_M \end{bmatrix} \quad \dots\dots (2)$$

With:
 $X_M = \frac{1}{n} \sum_{i=1}^n X_i$; $Y_M = \frac{1}{n} \sum_{i=1}^n Y_i$; $Z_M = \frac{1}{n} \sum_{i=1}^n Z_i$

Where:

n = the number of common points
 X_M, Y_M, Z_M = the mean of the Cartesian coordinates of “common” points in the local datum.
 X, Y, Z = Cartesian coordinates in the global datum
 $\Delta X, \Delta Y, \Delta Z$ = the translation parameters
 R_x, R_y, R_z = the rotation parameters
 ΔL = the scale factor
 X', Y', Z' = Cartesian coordinates in the local datum

The Study Area



PARAMETER SETS UNDER STUDY

PARAMETER	SPDC	CHEVRON	EXXON-MOBIL	AGIP	DMA	NORTEC	KARIALA	ELF
ΔX	+111.916m±2.3m	+92.968m	+94.031m	+111.916m	92m±3m	+93.200m	+113.936±1.21m	+88.98
ΔY	+88.852m±2.3m	+89.582m	+83.317m	+87.852m	93m±6m	93.310m	+88.918±1.21m	+83.23
ΔZ	-114.499m±2.3m	-116.39m	-116.708m	-114.499m	-122m±5m	-121.156m	-113.701±1.21m	-133.55
Rx	-1.87527±0.33"			-1.87527"		-1.93"	+1.881±0.55"	
Ry	-0.20214±1.61"			-0.20214"		-0.41"	0.204±0.10"	
Rz	-0.21935±0.19"			-0.21935"		+0.14"	+0.2222±0.11"	
Scale(ppm)	-0.03245±0.20			-0.03245		-21.2688	-0.017±0.17	

PARAMETER	FAJEMIROKUN	EZEIGBO	AGAJELU
ΔX (m)	-160.4±0.1	-92.9±1.6	-90.1±1.8
ΔY (m)	-67.4±0.0	-116.0±2.3	-107.7±1.8
ΔZ (m)	144.0±0.0	116.4±2.4	116.9±1.8
Rx	00° 4±3.0	00° 33±1.1	00° 08±0.8
Ry	1° 20±4.6	04° 20 ±1.7	-00° 35 ±01.3
Rz	01° 70±3.7	01° 70±1.5	-01° 73±0.8
Scale(ppm)	1 ± 1.4	20± 6	3.43 ± 1.3

Data Used for Study

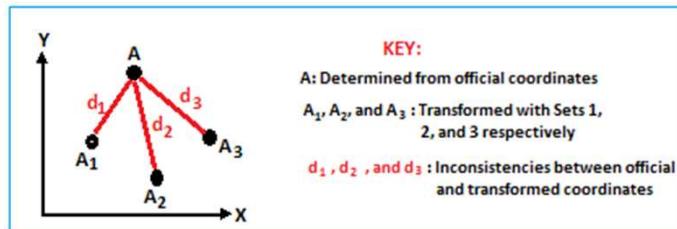
OFFICIAL COORDINATES OF COMMON POINTS (degree decimals)

S/NO	STATION ID	MINNA DATUM COORDINATES			WGS 84 (ITRF 2008) COORDINATES		
		LATITUDE	LONGITUDE	HEIGHT(Mean Sea Level) m	LATITUDE	LONGITUDE	HEIGHT (Ellipsoidal) m
1.	CP1	07 12 14.635	03 20 44.397	195.378	07 12 15.833	03 20 41.619	198.168
2.	CP2	05 07 17.371	08 20 22.008	111.265	05 07 19.304	08 20 19.778	105.584
3.	CP3	06 37 35.451	03 19 26.009	68.256	06 37 36.847	03 19 23.227	70.634
4.	CP4	07 48 26.201	06 42 49.262	438.934	07 48 27.462	06 42 46.824	437.548
5.	CP5	07 27 44.488	08 36 13.662	366.022	07 27 45.803	08 36 11.535	362.025
6.	CP6	09 38 19.885	06 33 33.980	471.012	09 38 20.581	06 33 31.311	470.679
7.	CP7	04 50 50.575	07 02 54.441	39.941	04 50 52.685	07 02 52.134	35.590
8.	CP8	05 32 19.445	05 44 18.970	25.970	05 32 21.410	05 44 16.472	23.590

INTERPOLATION METHODS APPLIED

- ▶ **1. Kriging Interpolation Method**
 - It measures the relationships between all of the sample points and then applies sophisticated statistical methods to predict the value of an unknown cell.
- ▶ **2: Inverse Distance Weighted Interpolation Method**
 - The Inverse Distance Weighted (IDW) interpolation method assumes that the nearer a sample point is to the cell whose value is to be estimated, the more closely the cell's value will resemble the sample point's value.

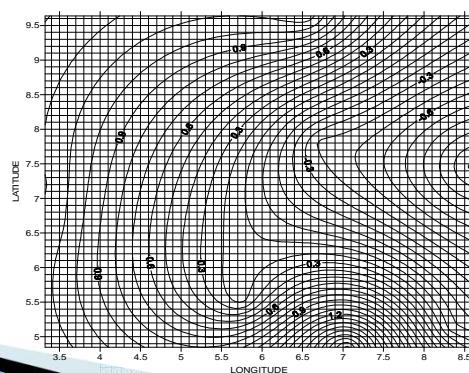
Estimation of Inconsistencies



- ▶ Magnitudes of the inconsistencies (dx , dy , and dz) were determined by computing the difference between the official Minna datum coordinates (X_o) of a point (obtained from OSGoF) and the corresponding Minna datum coordinates (X_T) transformed from WGS 84 datum using a Transformation set.
 - $dx = X_o - X_T$
 - $dy = Y_o - Y_T$
 - $dz = Z_o - Z_T$

REMOVAL OF INCONSISTENCIES (1)

- ▶ Two Steps Adopted:
 1. Inconsistencies determined at 8 common points were used to estimate the corresponding inconsistencies at the nodes of 90 grid cells using Kriging interpolation method.



REMOVAL OF INCONSISTENCIES (2)

2. The IDW (Inverse Distance Weighted) interpolation method uses the inconsistencies at the grid nodes to estimate the correction (dX_{cor}) for inconsistencies at any given point as follows:

$$X_I = X_T + dX_{cor}$$

$$Y_I = Y_T + dY_{cor}$$

$$Z_I = Z_T + dZ_{cor}$$

Where,

X_I = improved X coordinate

X_T = transformed X coordinate

Modified Approach

- One disadvantage of the approach shown so far is that a different set of Kriging charts has to be prepared for each transformation set.
- In order to have one set of charts for ALL the transformation sets, we made some modifications.
- In the modified approach:
 - instead of computing the inconsistencies (dx) at each grid node, the improved coordinates (X_I) of the grid node are determined.
 - For any transformation set, the transformed coordinates (X_T) (of a grid node) are compared with its corresponding X_I to yield the correction (dX_{cor}) at the node:

$$dX_{cor} = X_I - X_T.$$
 - Note: the magnitude of dX_{cor} at a point will vary according to the set used.
 - The IDW (Inverse Distance Weighted) interpolation method then uses the dX_{cor} at the grid nodes to estimate the correction (dX_{cor}) at any given point (as shown earlier).

RESULTS(3)

Table 6: Discrepancies after applying corrections (dx, dy, dz)

STN	COMP ONEN TS	NEW DISCREPANCIES										
		SPDC	CHEVRO N	EXXON- MOBIL	AGIP	DMA	NORTEC	KARIA LA	ELF	FAJEMI ROKUN	EZEIGB O	AGAJEL U
CP1	dx	0	0.001	0.001	0	0.001	0.003	-0.065	-0.058	0.005	-0.062	-0.06
	dy	-0.049	-0.058	-0.058	-0.049	-0.058	-0.043	0.031	0.029	-0.058	0.007	0.026
	dz	0.028	0.029	0.029	0.028	0.029	0.047	0.027	0.024	0.028	0.047	0
CP2	dx	0.021	0.024	0.0236	0.021	0.024	0.035	0	0.005	0.048	0.059	0.009
	dy	0.009	0.005	0.005	0.009	0.005	-0.043	0.002	0.026	0.011	0	0.024
	dz	0.05	0.0262	0.026	0.05	0.026	0.063	-0.006	-0.008	0.018	0.005	-0.027
CP3	dx	-0.01	-0.008	-0.008	-0.01	-0.008	0	0.151	0.152	0.01	0.196	0.157
	dy	0.151	0.152	0.152	0.151	0.151	0.107	-0.053	-0.033	0.157	-0.043	-0.034
	dz	-0.013	-0.033	-0.033	-0.013	-0.033	-0.012	-0.187	-0.186	-0.039	-0.199	-0.185
CP4	dx	-0.186	-0.186	-0.186	-0.186	-0.186	-0.176	0	-0.001	-0.19	-0.002	-0.006
	dy	-0.001	-0.001	-0.001	-0.001	-0.001	0.007	0.002	-0.001	0.003	-0.012	0
	dz	-0.003	-0.001	0	-0.003	-0.001	-0.002	-0.018	-0.009	-0.003	-0.089	0.061
CP5	dx	0.002	-0.008	-0.008	0.002	-0.008	-0.023	0.001	-0.011	-0.079	-0.167	-0.031
	dy	-0.023	-0.011	-0.011	-0.023	-0.011	0.139	-0.006	-0.076	-0.02	-0.024	-0.069
	dz	-0.146	-0.076	-0.076	-0.146	-0.076	-0.179	-0.006	-0.012	-0.057	0.156	-0.008
CP6	dx	-0.018	-0.012	-0.012	-0.018	-0.012	-0.051	0.002	0.076	0.02	0.019	0.075
	dy	0.149	0.076	0.076	0.149	0.076	0.187	0.005	-0.012	0.05	-0.148	-0.04
	dz	-0.029	-0.012	-0.012	-0.029	-0.012	0.139	0.001	0.01	-0.011	-0.176	0.027
CP7	dx	0.018	0.01	0.01	0.018	0.01	0.04	-0.001	-0.077	-0.045	-0.072	-0.082
	dy	-0.152	-0.077	-0.077	-0.152	-0.077	-0.137	-0.004	-0.01	-0.056	0.14	0.019
	dz	-0.016	-0.01	-0.01	-0.016	-0.01	-0.188	-0.001	0.006	-0.005	-0.055	0.041
CP8	dx	0.01	0.006	0.006	0.01	0.006	0.002	0.001	-0.012	-0.035	-0.089	-0.023
	dy	-0.026	-0.012	-0.012	-0.026	-0.012	0.057	0.003	-0.033	-0.015	0.006	-0.027
	dz	-0.069	-0.033	-0.033	-0.069	-0.033	-0.102	-0.065	-0.058	-0.023	-0.062	-0.06

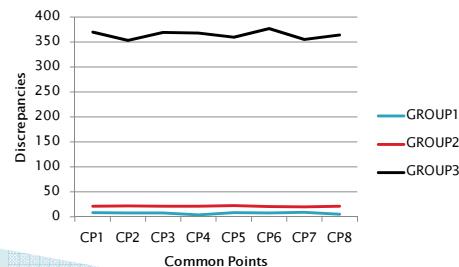
RESULTS(4)

Table 7: 3-D discrepancies before and after applying corrections ("OLD" and "NEW" respectively)

STN	DISCR EPANC IES (m)	TRANSFORMATION SETS										
		SPDC	CHEVRO N	EXXON- MOBIL	AGIP	DMA	NORTEC	KARIA LA	ELF	FAJEMIR OKUN	EZEIGB O	AGAJEL U
CP1	OLD	8.362	21.666	22.389	8.498	24.773	26.749	5.694	35.354	407.662	370.292	362.388
	NEW	0.056	0.064	0.065	0.056	0.065	0.064	0.077	0.069	0.065	0.078	0.065
CP2	OLD	8.200	22.252	21.207	7.315	25.879	23.905	5.237	34.190	401.521	353.254	361.714
	NEW	0.055	0.036	0.035	0.055	0.036	0.084	0.006	0.028	0.052	0.059	0.037
CP3	OLD	8.082	21.658	22.425	8.174	24.673	26.723	6.411	35.240	407.797	369.297	362.594
	NEW	0.152	0.156	0.156	0.152	0.155	0.108	0.246	0.242	0.162	0.283	0.245
CP4	OLD	4.231	21.582	21.192	3.859	23.528	23.120	3.344	31.060	409.082	368.476	367.112
	NEW	0.186	0.186	0.186	0.186	0.186	0.176	0.018	0.009	0.190	0.090	0.061
CP5	OLD	8.761	23.005	21.119	7.903	26.025	23.477	3.592	32.164	404.358	360.131	363.990
	NEW	0.148	0.077	0.077	0.148	0.077	0.228	0.009	0.078	0.099	0.230	0.076
CP6	OLD	8.018	20.783	22.350	8.837	21.057	19.743	8.507	30.232	412.765	377.434	371.632
	NEW	0.153	0.078	0.078	0.153	0.078	0.239	0.005	0.078	0.055	0.231	0.089
CP7	OLD	8.980	20.091	18.549	7.987	23.308	25.031	2.291	30.409	403.128	355.595	361.690
	NEW	0.154	0.078	0.078	0.154	0.078	0.236	0.004	0.078	0.072	0.167	0.094
CP8	OLD	5.118	21.373	21.020	4.323	23.496	26.001	5.096	31.311	408.546	364.3	365.736
	NEW	0.074	0.036	0.036	0.074	0.036	0.117	0.065	0.068	0.044	0.109	0.070
Mean Value	OLD	7.469	21.551	21.281	7.112	24.092	24.344	5.022	32.495	406.857	364.847	364.607
Mean Value	NEW	0.122	0.089	0.089	0.122	0.089	0.157	0.054	0.081	0.092	0.156	0.092
		Overall Mean, (m)										OLD 116.334 NEW 10.104

DISCUSSIONS OF RESULTS(1)

- ▶ From the discrepancies shown in Tables 4 and 7, it can be noticed that the transformation sets can be categorized into three in accordance with the magnitudes of their discrepancies as follows:
 - GROUP 1: Kariala, Agip, and SPDC transformation sets which gave mean discrepancies within the range 5m to 7.5metres.
 - GROUP 2: Exxon-Mobil, Chevron, DMA, Nortec, and ELF where mean discrepancies are within the range 21.3m – 32.5m.
 - GROUP 3: Agajelu, Ezeigbo, and Fajemirokun where the range of mean discrepancies is 364.6– 406.9m.



DISCUSSIONS OF RESULTS(2)

- ▶ Table 2 shows:
 - the Group1 transformation sets were derived from coordinates obtained from GPS re-observation of some National primary triangulation points sponsored by the SPDC[Fubara, 2011];
 - the Group2 sets comprise mainly of 3-parameter transformation sets (except for Nortec).
 - The Group3 sets are suspected to have been derived from Transit (Doppler) satellite data captured in the ADOS (African Doppler Survey) project which was computed on the WGS 72 datum and later transformed to WGS84 (Ezeigbo, 2004; Jackson, 2011).
 - This third category was deliberately included in this study to show the power of our method in improving results obtained from transformation sets derived from heterogeneous data.

DISCUSSIONS OF RESULTS(3)

- Tables 5, 6 and 7 show the capability of our method to reduce the absolute discrepancies from 35m to a mean value of 0.104 metres (10.4 cm) for all the transformation sets (shows 2nd-order improvement) (Fig 4).

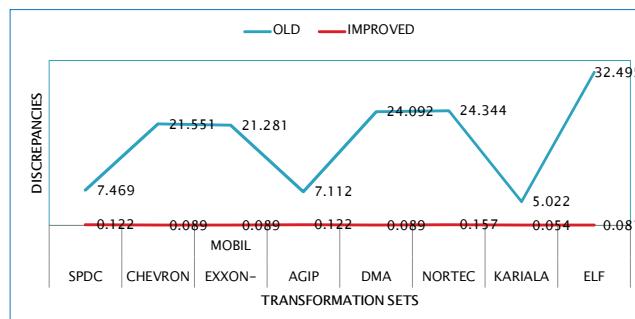


Fig. 4

CONCLUSION AND RECOMMENDATIONS

- From the discussions above, the following conclusions can be drawn:
- Our method was able to reduce the inconsistencies between the different transformation set studied from the level of 35metres to 0.104metres (10.4cm). The method can therefore use any of the transformation sets to transform the WGS84 coordinates of any given point into the Minna datum (and vice-versa) with mean accuracy of 0.104m (10.4cm).
- With our method it is possible to transform the Minna datum curvilinear coordinates (ϕ, λ, H) of existing primary triangulation points in Nigeria to the WGS84 datum (and consequently to the African geodetic Reference Frame, AFREF) with accuracy better than 0.104m (10.4cm).
- The method is therefore recommended for the reduction of the inconsistencies arising from the multiplicity of transformation sets currently used by the various petroleum exploration companies in Nigeria to the level of 10.4cm.

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► THANK YOU