# A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid

# **Products – Preliminary Results**

# ZHENG Zuoya, P. R. China, CHEN Yongqi, Hong Kong SAR, China YI Zhonghai, P. R. China

Keyword: GPS Ultra-Rapid Ephemeris, Satellite Clock Bias Prediction, Real-time PPP

#### SUMMARY

GPS real time precise point positioning (RT-PPP) requires real-time, accurate and reliable prediction of satellite clock biases (SCBs). This is one of the most challenging tasks in the development of a RT-PPP technique. Several approaches have been developed, like the grey model (GM), linear model (LM) and quadratic polynomial model (QPM). The abovementioned approaches are discussed and compared using real data in this paper. We predicted the 24-hour SCBs using the IGS ultra-rapid products in the previous day. This paper compared the IGS predictions with those obtained with the GM, LM and QPM methods.

From the testing and analyzing the data of two adjacent days, some preliminary observations are made as follows.

- The predicted SCBs from the previous-day observations with the LM have similar accuracy as the IGS products;
- The QPM can not generate better results than the IGS products;
- We can get more accurate predictions with the GM as long as the EC is properly selected. This is the area worth exploring.

TS 4B – GNSS 1

# A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid

#### **Products – Preliminary Results**

# ZHENG Zuoya, P. R. China, CHEN Yongqi, Hong Kong SAR, China YI Zhonghai, P. R. China

#### **1. INTRODUCE**

The Analysis Centers of the IGS offer precise GPS ephemeris for post-processing. It is well known that the accuracy of orbit products is better than 5cm, and that of satellite clock bias (SCB) approaches 0.1ns (<u>igscb.jpl.nasa.gov</u>), which can meet the requirements of cm-level precise point positioning (PPP). However, IGS final products have a latency of 13 days (see in Table 1), and therefore can not meet the need of RT- PPP. For RT mode, only are the broadcast and the ultra-rapid (predicted) applicable, but the accuracy of the former is low. Therefore development of an approach to predict SCBs is of particular importance in the RT-PPP.

There are two commonly used schemes to predict SCBs. One is to predict the SCBs using the SCBs of the previous day obtained from IGS ultra-rapid products (observed), the other is to predict SCBs with other prediction means (e.g., Senior, et al 2001; Dounis, et al 2005). We prefer to first scheme because the ultra-rapid observations are ready available. In this paper we first analyze the SCBs in IGS ultra-rapid products, including the differences and correlations between the SCBs in two adjacent days. Three prediction models, i.e., grey model (GM), linear model (LM) and quadratic polynomial model (QPM), are then discussed and compared using real data. The results also were compared with the IGS predicted values. Some observations are finally given.

		accuracy	latency	update	Sample interval	
Dreadaast	Orbit	160cm	рт		doilte	
Broadcast	Sat. Clock	7ns	KI		dally	
Ultra-Rapid	Orbit	10cm	PT 4 ti		15 min	
(predicted half)	Sat. Clock	5ns	KI	daily	1,511111	
Ultra-Rapid	Orbit	<5cm	2 hours	4 times	15	
(observed half)	Sat. Clock	0.2ns	5 Hours	daily	1511111	
Danid	Orbit	<5cm	17hours	doily	15min	
карій	Sat. Clock	0.1ns	1/nours	uany	5min	
Final	Orbit	<5cm	13 days	weekly	15min	

**Table 1.** IGS Products (GPS Satellite Ephemeris and Clock Bias)

TS 4B – GNSS 1

Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products – Preliminary Results

Strategic Integration of Surveying Services FIG Working Week 2007 Hong Kong SAR, China, 13-17 May 2007

Sat. Clock 0.1ns 5m	in
---------------------	----

# 2. ANALYSIS OF SCBS IN IGS ULTRA-RAPID PRODUCTS

The official IGS products showed in Table 1 are the weighted averages of the results obtained from the Analysis Centers (Jay Oaks, Ken Senior, et al 2003; V. Broderbauer, R. Weber, 2003). To understand better the relationship between two adjacent-day SCB observations, predictions and final values, we used the SCB data of 7<sup>th</sup> and 8<sup>th</sup> Dec. 2004 and analyzed their differences and correlations.

# 2.1 The Differences between the Predicted and Final SCBs

Taking SCBs of satellite PRN-1 and PRN-8 as example: one has its SCBs increasing with time, and the other decreasing with time. We plotted the differences among the observed, predicted and final SCBs for those two days in Figure 1, where, the O-F means the differences in nanosecond between the observed and final results; the P-F is the differences between predicted and final; the P-O is the differences between the predicted and observed. It is showed that the differences between the observed and final SCBs are less than 2ns, using the final products with precision of 0.1-0.2ns as reference. It indicated the observed SCBs are quite accurate. The differences of the P-F or the P-O are about 20ns, indicating the precision of predictions is low. Figure 2 shows the results for PRN-8. The similar conclusions can be drawn. Hence, the predicted IGS ultra-rapid products are poor and can not be used for precise **RT-PPP**.



Fig.1 the differences among the predicted, observed and final SCBs for PRN-1

TS 4B – GNSS 1 Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products - Preliminary Results



Fig.2 the differences among the predicted, observed and final SCBs for PRN-8

### 2.2 Correlations between two Adjacent-day SCBs

To predict SCBs with the previous-day observed SCBs it is useful to analyze the correlations between the observed, predicted and final SCBs. Taking the SCBs of PRN-8 as example, Figure 3 plots the differences of the O-F for two days (left side) and that of the P-O (right side). One can see from the figures that there is a similar trend suggesting a strong correlation in the O-F between two adjacent days, but less in the P-O. The strong correlation implies that we can predict the SCBs using the previous-day observed values.



Fig.3 the differences between observed and final SCBs (left) and predicted and observed SCBs (right) for PRN-8 for two days



Fig.4 the differences of SCBs between two adjacent days for PRN-8

Figure 4 is another group of plots using SCBs data for PRN-8. The first and second plots in both left and right sides shows the observed SCBs for different days, and the differences between them, respectively. The third plot in the left side shows the final SCBs, and the third plot in the right side shows the predicted SCBs. The differences in the final SCBs between two adjacent days and in the predicted SCBs are shown in the fourth plot of left side and right side, respectively. Comparing the second and fourth plots in the left side and the right side, one can see that the differences of the observed SCBs between two days have a similar trend to the differences of the final SCBs, but not the case for the differences of the predicted SCBs. Table 2 gives the correlation coefficients between the two day's SCBs, where (O-F)[x]and (P-O)[x] stand the differences between the observed and final SCBs for day x, respectively, and O[7-8], F[7-8], and P[7-8] represent the differences between days 7 and 8 observed, final, and predicted SCBs, respectively. From the table it is clear that the two adjacent day differences between the observed and final SCBs exhibits a strong correlation, but not so for the differences between the predicted and observed SCBs. Also a strong correlation exists for the differences of two adjacent day's observed SCBs versus the differences of two adjacent day's final SCBs, while no clear indication for the predicted versus the observed.

Satallita	(O-F)[7] versus	(P-O)[7] versus	O[7-8] versus	P[7-8] versus
Saterine	(O-F)[8]	(P-O)[8]	F[7-8]	O[7-8]
PRN-1	0.9622	0.5237	0.9996	0.6484
PRN-3	0.9912	-0.5867	0.9995	-0.5282
PRN-8	0.9944	0.1785	0.9997	-0.2961
PRN-16	0.9945	-0.6054	0.9260	-0.0184
PRN-30	0.9920	0.9206	0.9995	0.9594

**Table 2**the correlation coefficients in adjacent day's SCBs

TS 4B – GNSS 1

Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products – Preliminary Results

Strategic Integration of Surveying Services FIG Working Week 2007 Hong Kong SAR, China, 13-17 May 2007

#### **3. SCB PREDICTION**

Three prediction models, i.e., the GM, LM, and QPM, will be used to predict the 24 hour-SCBs using the previous day's observed SCBs. The prediction accuracy will be evaluated.

#### 3.1 Grey Model (GM)

The grey model is discussed in detail in (Deng, 1987; Yan and Dai, 1989; Zhao, 1997; Jiao, 2003; and Cui, 2005). The modified GM by Zheng and Chen (2007) reads

$$\hat{x}^{(0)}(k+p) = \left[x^{(0)}(1) - \frac{b}{a}\right] e^{-a \cdot \lambda \cdot (k+p-1)} \cdot (1-e^{a})$$

Where, k is the number of original data used for prediction; p is the prediction point

and  $p \in Z$ ; a, b are constants;  $\lambda$  is an exponent coefficient (EC). Taking the SCB data of

PRN-1 on 7 Dec. 2004 as an example, we applied the GM to predict the SCBs of the adjacent-day (i.e., 8 Dec. 2004). Here the observed SCBs were used as references because they have small differences with the final products. We took k=10 as the number of initial epochs and 15 minutes as sampling interval. Figure 5 shows the predicted SCBs and the computed EC values using the reverse analysis method. The second plot in the left side of the figure tells the prediction error is about 5~10ns. Table 3 gives the statistics, where the P-O (Ultra) means the differences between observations and predictions from IGS Ultra-rapid products, and the P-O (GM) means the differences between observations and predictions with the GM. One can see that the prediction precision with the GM is better than that of Ultra-rapid product, and the accuracy of the GM-predicted SCBs is about 2-3ns, but about 10ns from the Ultra-rapid product.



Fig.5 the SCB predictions and model EC of PRN-1 on 7<sup>th</sup> Dec. 2004

TS 4B – GNSS 1 Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products - Preliminary Results

	Max (ns)	Min (ns)	Mean (ns)	Std (ns)
P-O (Ultra)	3.3240	-18.8910	-7.8584	5.5121
P-O (GM)	3.8422	-6.1804	-0.6438	2.5733
EC	2.12	1.46	1.93	0.25

 Table 3 the statistics of SCB prediction precision and model EC for PRN-1

Figure 6 shows the predicted values for PRN-1 on 8 Dec. 2004. In the left plots EC is fixed as 2.2. The EC values computed from the observed SCBs of 8 Dec. 2004, using the reverse analysis method, are plotted in the right side. One can see the EC values are significantly different from those on 7 Dec. It is therefore expected that the prediction accuracy using the EC of 7 Dec. is low.



Fig.6 the predicted SCBs and model EC for PRN-1 on 8 Dec. 2004

Figure 7 shows the differences in the prediction errors using different EC values. In the prediction the initial values were took the first 10 epochs of 8<sup>th</sup>. The left plots are the results with an average EC from the data on 7 Dec., while the right plots the results with corresponding EC values on 7 Dec. One can see that the different prediction results are obtained with different EC values, and the predictions precision is too low with the EC computed by the previous-day's SCB observations.



Fig.7 the SCB predictions of PRN-1 on  $8^{th}$  (left: with an average EC of  $7^{th}$ ; right: with corresponding EC of  $7^{th}$ )

Figure 8 gives the SCB predictions for two adjacent days (7<sup>th</sup> and 8<sup>th</sup>) with the EC computed by SCB observations on 7<sup>th</sup>. The initial values are at the first 10 epochs of 7<sup>th</sup>. From the left plots, we can see the prediction errors increase rapidly when predictions are made for 8<sup>th</sup>. The right plot shows the ECs computed from the IGS ultra-rapid observations on 7<sup>th</sup> and 8<sup>th</sup>. It is obvious that EC values for both days are not correlated. The statistics of SCB predictions and model EC of PRN-1 on 8<sup>th</sup> are given in table 4.



Fig.8 the SCB prediction and model EC of PRN-1 at 7<sup>th</sup> and 8<sup>th</sup>

	Max	Min	Mean	Std
P-O (Ultra)	13.5219	-5.0710	4.4704	4.1799
P-O(GM)2.2	11.6770	-6.9395	4.2645	4.8789
P-O(GM) average	8.9629	-26.9629	-6.2155	9.7608
P-O(GM) Corresponding	8.2244	-23.8212	-5.6662	9.0345
EC	2.34	0.66	1.92	0.41

Table 4 the statistics of SCB prediction and model EC of PRN-1 at 8<sup>th</sup>

TS 4B – GNSS 1

Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products – Preliminary Results

Strategic Integration of Surveying Services FIG Working Week 2007 Hong Kong SAR, China, 13-17 May 2007

#### 3.2 Linear model (LM)

We used the LM based on the SCB observations of 7<sup>th</sup> to predict the SCB of 8<sup>th</sup>. Figure 9 shows the residuals of SCBs after fitting a linear function into the data (left plot) and the discrepancies between the predict SCBs of the 8<sup>th</sup> and the observations (right plot). Table 5 lists the statistics. The results tell us that the precision of prediction (Std) using the LM is about 5.7ns, lower than IGS prediction. However, there is a significant bias of 4.5ns in the IGS predictions. The accuracy of the prediction with the LM is therefore higher.



Fig.9 Prediction of 8<sup>th</sup> SCBs based on a LM fitting to the data from 7<sup>th</sup> Dec. 2004

		0 1			
	LM	Max	Min	Mean	Std
7	P-O (Ultra)	3.3240	-18.8910	-7.8584	5.5121
	P-O (Ployfit)	6.1160	-7.0168	0	2.9759
8	P-O (Ultra)	13.5219	-5.0710	4.4704	4.1799
	P-O (Predict)	8.7475	-15.0471	-0.2785	5.6836

Table5 the fitting and prediction statistics with the LM

### 3.3 Quadratic Polynomial Model (QPM)

Similar to the LM, we used the QPM to fit a quadratic polynomial function into the data of the 7<sup>th</sup>. The estimated function was then used to predict the SCBs of the 8<sup>th</sup>. The results are in Figure 10 and table 6. It is clear that the results are not as good as those with the LM.

Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products – Preliminary Results



Fig.10 Predicting 8<sup>th</sup> SCB according to QPM fitted from 7<sup>th</sup> Dec. 2004

	QPM	Max	Min	Mean	Std
7	P-O (Ultra)	3.3240	-18.8910	-7.8584	5.5121
	P-O (Ployfit)	4.5566	-4.9961	0	2.4470
8	P-O (Ultra)	13.5219	-5.0710	4.4704	4.1799
	P-O (Predict)	39.3848	-1.8073	22.3285	10.8388

Table 6 the fitting and prediction residual statistics with QPM

Table 7 summarizes the results for other satellites. When measuring the accuracy of the predicted values two components of the Std and the bias must be taken into account. From the table one can conclude that in general, the QPM predicted SCBs have lower accuracy than the IGS predictions, and the LM produces the SCBs with similar accuracy to the IGS predictions.

<b>G</b> .	T.		LM				QPM			
Sat.	Time	Method	Max	Min	Mean	Std	Max	Min	Mean	Std
	7	P-O (Ultra)	9.2140	0.9450	5.0954	2.4319	9.2140	0.9450	5.0954	2.4319
DDN 2	/	P-O (Ployfit)	2.2647	-3.2010	0	1.2782	2.2836	-3.0807	0	1.2733
PKIN-3	0	P-O (Ultra)	5.5600	-9.7489	-3.7058	4.0162	5.5600	-9.7489	-3.7058	4.0162
	8	P-O (Predict)	7.4437	.10.2702	2.6100	4.1438	6.8339	-11.5840	4.0934	4.6994
	7	P-O (Ultra)	6.9199	-0.05199	2.8181	1.6533	6.9199	-0.05199	2.8181	1.6533
DDN 9		P-O (Ployfit)	3.3040	-3.9879	0	1.4799	3.3912	-4.0931	0	1.4651
FKIN-0	0	P-O (Ultra)	5.4509	-6.8889	-0.9107	3.6734	5.4509	-6.8889	-0.9107	3.6734
	8	P-O (Predict)	5.3204	-6.5887	1.3065	3.5088	7.5653	-2.7162	1.4807	2.6244
PRN-16	7	P-O (Ultra)	1.6639	0.0960	0.8352	0.4271	1.6639	0.0960	0.8352	0.4271
		P-O (Ployfit)	0.3728	-0.5476	0	0.1888	0.3899	-0.5379	0	0.1871
	8	P-O (Ultra)	-0.2989	-1.3190	-0.9246	0.2525	-0.2989	-1.3190	-0.9246	0.2525

Table7 the statistics of the SCB predictions with the LM and QPM

TS 4B – GNSS 1

Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products – Preliminary Results

Strategic Integration of Surveying Services FIG Working Week 2007 Hong Kong SAR, China, 13-17 May 2007

		P-O (Predict)	-0.2874	-1.1982	0.8088	0.2040	-0.3459	-1.6130	1.1493	0.2816
	7	P-O (Ultra)	7.1110	-0.0060	4.1524	1.8166	7.1110	-0.0060	4.1524	1.8166
DDN 20	/	P-O (Ployfit)	0.9684	-1.4057	0	0.5633	0.8662	-1.0729	0	0.5202
PKIN-30	8	P-O (Ultra)	6.1799	-0.7549	2.1653	1.8332	6.1799	-0.7549	2.1653	1.8332
		P-O (Predict)	9.1972	-0.3974	3.8953	2.5176	15.402	0.0985	6.7802	4.1914

# 4. CONCLUSIONS

The IGS produces SCB predictions, which are the weighted average of the results obtained by the IGS Analysis Centers. Each center may use different prediction methods. This paper compared the IGS predictions with those obtained with the GM, LM and QPM methods.

From the testing and analyzing the data of two adjacent days, some preliminary observations are made as follows.

- The predicted SCBs from the previous-day observations with the LM have similar accuracy as the IGS products;
- The QPM can not generate better results than the IGS products;

- We can get more accurate predictions with the GM as long as the EC is properly selected. This is the area worth exploring.

# ACKNOWLEDGEMENT

This study was supported by Research Grants Council of Hong Kong (PolyU B-Q934) and Open Research Fund Program of the Key Laboratory of Geomatics and Digital Technology, Shandong Province (SD060804)

# REFERENCES

A.I Dounis, P.Tiropanis, et al (2005), A comparison of Grey Model and Fuzzy Predictive Model for Time series, International Journal of Computational Intelligence, IJCI, Volume 2 Number 3, ISSN, P176-181.

CUI Xianqiang, JIAO Wenhai (2005), Grey System Model for the Satellite Clock Error Predicting, Geomatics and Information Science of Wuhan University, WUHAN, Vol.30, No.5, P447-450.

DENG Julong (1987), Grey System Method [M], Wuhan: Huazhong University of Science and Technology Press.

Jay Oaks, Ken Senior et al (2003), Gloabal Positioning System Constellation Clock Performance, 35th Annual Precise Time and Time Interval (PTTI) Meeting. California, P: 173-184.

JIAO Wenhai (2003), Researches on the Realization of Satellite Navigation Coordinate TS 4B – GNSS 1 11/13

Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products – Preliminary Results

Reference System [R], post-doctoral dissertation, Shanghai: Shanghai Astronomical Observatory, CAS.

Ken Senior Paul Koppang, et al (2001), Development an IGS Time Scale, Preprint for Proceeding of the IEEE/EIA International Frequency Control Symposium. USA Seattle, P: 1-8.

V. Broderbauer, R. Weber (2003), Results of Modeling GPS Satellite Clocks, Geoinfo. 91(1): 38-47.

YAN Zhiyuan, DAI Yusheng (1989), Grey System Prediction and Application [M], Nanjing: Jiangsu Science and Technology publishing house.

ZHAO Yunsheng (1997). Grey System Theory and its Application in Geoscience [M]. Wuhan: Huazhong University of Science and Technology.

Zuoya ZHENG, Yongqi CHEN, et al (2007). Improved Grey Model and Application in Real-Time GPS Satellite Clock Bias Prediction. Chinese Journal of Geophysics (in review).

### **BIOGRAPHICAL NOTES**

Zheng Zuoya, male, was born in 1978, Ph.D, Chinese, Research major: GNSS integration and applications, Spatial Aero-craft Precise Orbit Determination and its application, Spatial Geodesy and Geodynamics.

Chen Yongqi, male, was born in 1943, Professor, Ph.D, Hong Kong. Research major: GPS data processing, Marine Surveying, Urban Hazards Mitigation, Navigation and so on. Chair Professor and Head of Department of Land Surveying and Geo-Informatics, the Hong Kong Polytechnic University.

### **CONTACTS**

Zheng Zuoya Department of Land Surveying and Geo-Informatics HJ715, the Hong Kong Polytechnic University Hung Hom, Kowloon, Hong Kong Tel: + 852-6575 2416 Fax: +852-2330 2994 Email: caszzy@gmail.com

Chen Yongqi Department of Land Surveying and Geo-Informatics HJ704, the Hong Kong Polytechnic University, Hung Hom

TS 4B – GNSS 1 Zuova Zheng, Yongqi Chen and Mr. Zhonghai Yi A Study on the Prediction of GPS Satellite Clock Bias with IGS Ultra-rapid Products - Preliminary Results

Strategic Integration of Surveying Services FIG Working Week 2007 Hong Kong SAR, China, 13-17 May 2007

Kowloon HONG KONG Tel: +852-2766 5966 Fax: +852-2330 2994 Email: <a href="https://www.emailton.com">lsyqchen@polyu.edu.hk</a>